Alaska-DLM Essential Elements and Instructional Examples for Mathematics

Eighth Grade

Revised for Alaska July, 2014







The present publication was developed under grant 84.373X100001 from the U.S. Department of Education, Office of Special Education Programs. The views expressed herein are solely those of the author(s), and no official endorsement by the U.S. Department should be inferred.

AK-DLM ESSENTIAL ELEMENTS AND COMPLEXITY EXAMPLES FOR EIGHTH GRADE

Eighth Grade Mathematics Standards: The Number System

AK Grade-Level Clusters	AK-DLM Essential Elements	Instructional Examples
Know that there are	EE8.NS.1. Subtract	Students will:
numbers that are not	fractions with like	EE8.NS.1. Subtract fractions with like denominators (halves, thirds,
rational, and approximate	denominators (halves,	fourths, and tenths) with minuends that may be greater than one.
them by rational numbers.	thirds, fourths, and tenths)	Ex. Subtract two fractions with like denominators with models or numbers.
	with minuends less than or	Ex. If I have 1 3/4 and I take 1/4 away, how many wholes and fourths are
8.NS.1. Know that numbers	equal to one.	left?
that are not rational are		
called irrational.		Students will:
Understand informally that		EE8.NS.1. Subtract fractions with like denominators (halves, thirds,
every number has a		fourths, and tenths) with minuends less than or equal to one.
decimal expansion; for		Ex. Use fraction bars or fraction circles to add and match a numerical
rational numbers, show		representation to the model so the answer is less than or equal to one.
that the decimal expansion		Ex. Given 3/4, take 1/4 away and tell or show how many fourths are left.
repeats eventually, and		Ex. Given 7/10, recognize that 3/10 are needed to make a whole. (Connect
convert a decimal		to money – 10 dimes = one whole dollar.)
expansion which repeats		
eventually into a rational		Students will:
number.		EE8.NS.1. Use models to subtract halves, thirds, and fourths.
		Ex. Given a whole divided into thirds, tell how many times they can take a
		third out of the whole.
		Ex. Presented a rectangle with 1/3 of the whole shaded, tell how many
		thirds are left.
		Students will:
		EE8.NS.1. Use models to identify the whole and find the missing pieces of
		a whole using halves.
		Ex. Presented an object with a piece missing and a whole object, identify

AK Grade-Level Clusters	AK-DLM Essential Elements	Instructional Examples
		the whole. Ex. Given 1/2 of a pizza, identify the missing part (concrete model or touch board). Ex. Given a whole with 1/2 shaded, identify the missing part.
8.NS.2. Use rational approximations of irrational numbers to compare the size of irrational numbers, locate them approximately on a number line diagram, and estimate the value of ĞdžĐđĞEEŝŽŶE;ĞŐ v²). For example, by truncating the ĚĞĐŝŵĂů ĞđĐĂŶEŝŽŶ ŽĨ AŢ show tŚĂt ATŜE dĞt//ĞĞŶ 6 and 2, then between 1.4 and 1.5, and explain how to continue on to get better approximations.	FEB.NS.2.a. Express a fraction with a denominator of 100 as a decimal. EEB.NS.2.b. Compare quantities represented as decimals in real-world examples to hundredths.	EE8.NS.2. Represent different forms and values of decimal numbers to the hundreds place (decimal, fraction, hundreds grid, and money representation). Ex. Given a hundreds grid, shade in an approximation to a given decimal or fraction. Ex. Given a picture of a shaded hundreds grid, determine the decimal or fractional part. Ex. When given coins representing 60 cents, write the decimal amount as \$0.60. Students will: EE8.NS.2. Represent different forms and values of decimal numbers using fractions with numerators that are multiples of five and a denominator of 100. Ex. Given a hundreds grid with one fourth shaded-in, identify the correct decimal representation from choices 25/100, 10/100, or 100/100. Ex. When given coins representing 50 cents, write the decimal value as \$0.50. Students will: EE8.NS.2. Distinguish between a part represented by a decimal and a

AK Grade-Level Clusters	AK-DLM Essential Elements	Instructional Examples
		Ex. Given a dollar and two quarters, identify which represents the whole (dollar) and the decimal part (two quarters). Ex. Given a fully shaded-in hundreds grid and a partially shaded-in hundreds grid, identify which represents the whole and which represents the decimal (part of a whole).
		Students will: EE8.NS.2. Identify a part of a whole in concrete real-world objects. Ex. When shown an apple with a missing piece, identify the part that is missing. Ex. When given a student's schedule for the day with one activity missing, identify what activity is missing from their schedule. Ex. Show which piece is missing from a familiar object.

Eighth Grade Mathematics Standards: Expressions and Equations

AK Grade-Level Clusters	AK-DLM Essential Elements	Instructional Examples
Expressions and	EE8.EE.1. Identify the	Students will:
Equations. Work with	meaning of an exponent	EE8.EE.1-4. Use powers of 10 to compose and decompose numbers.
radicals and integer	(limited to exponents of 2 and 3).	Ex. Recognize 3 x 10^2 = 300 as another way to state 3 x 100 = 300.
	EE.8.EE.2. Identify a	
	geometric sequence of	
	whole numbers with a	
	whole number common	
	ratio.	
	EE.8.EE.3-4. Compose and	
	decompose whole	
	numbers up to 999.	
exponents.		irrational.
8.EE.1. Know and apply the		8.EE.3. Use numbers expressed in the form of a single digit times a whole-
properties of integer		number power of 10 to estimate very large or very small quantities, and to
exponents to generate		express how many times as much one is than the
equivalent numerical		
expressions. For example,		
$3^2 \times 3^{-5} = 3^{-3} = 1/3^3 = 1/27.$		
8.EE.2. Use square root		
and cube root symbols to		
represent solutions to		
equations of the form $x^2 =$		
p and $x^3 = p$, where p is a		
positive rational number.		
Evaluate square roots of		
small perfect squares and		
cube roots of small perfect		

Ex. $5 \times 10^1 = .$	100, 3 = 30, and 4 = 1).
Students will:	Ex. Given two nickels, show the correct number to represent that va
EE8.EE.1-4.	
Compose and	Students will:
decompose	EE8.EE.1-4. Recognize the specific value a number represents.
numbers to	Ex. Recognize a number using pictorial representations.
three digits.	Ex. Match a numerical value with a pictorial representation or concr
Ex. 300 + 50 +	objects.
7 = .	Ex. Look at a model and determine the numeric value.
Ex. 57 =+	Ex. Given a jig or a model with 10 spaces, put one object per space a
Ex. Show that twelve is	assemble a group of 10.
one 10 and two ones,	Ex. Given three bears, select the number three card.
or 12 ones, or seven	
ones and five ones, etc.	
Students will:	
EE8.EE.1-4. Use	
models to	
represent the	
composition of	
numbers. Ex.	
Illustrate a	
number using	
models. Ex. Show	
that 12 is one 10	
and two ones. Ex.	
Compose	
numbers to five.	
Ex. Compose numbers to 10.	
Ex. Model numbers using	
base ten blocks.	

Ex. Distinguish the value of the digits in 134 (e.g., 1 =

AK Grade-Level Clusters	AK-DLM Essential Elements	Instructional Examples
other. For example, estimate the population of the United States as 3 times 10 ⁸ and the population of the world as 7 times 10 ⁹ , and determine that the world population is more than 20 times larger. 8.EE.4. Perform operations		
with numbers expressed in scientific notation, including problems where both decimal and scientific		
notation are used. Use scientific notation and choose units of		
appropriate size for measurements of very		
large or very small quantities (e.g., use		
millimeters per year for seafloor spreading). Interpret scientific notation		
that has been generated by technology.		
	EE8.EE.5-6. Graph a simple	Students will:
connections between		EE8.EE.5-6. Graph a simple ratio using the x and y axis points when given
proportional relationships,	,	the ratio in standard form (2:1) and expand on the ratio by two or more
lines, and linear equations.		points.
	the y/x.	Ex. Given a ratio 2:1 (there are two balloons for every child), graph the
8.EE.5. Graph proportional		linear equation on a graph labeled x axis and the y axis. This equation

AK Grade-Level Clusters	AK-DLM Essential Elements	Instructional Examples
relationships, interpreting		would have a slope of 2.
the unit rate as the slope		Ex. Given there is one boy for every one girl, graph points for the ratio of
of the graph. Compare two		1:1 (this linear equation will have a slope of 1).
different proportional		Ex. Given two plotted data points, plot a third point using pictures.
relationships represented		Ex. Given a ratio of 3:1 indicating that each student needs three items,
in different ways. For		convert the ratio to fraction form (2/1) and plot on a pre-labeled graph
example, compare a		this point and two additional points that are functions of the original ratio
distance-time graph to a		(3:1, 6:2, 9:3).
distance-time equation to		
determine which of two		Students will:
moving objects has greater		EE8.EE.5-6. Graph a simple ratio using the x and y axis points when given
speed.		the ratio in standard form (2:1) and convert to 2/1.
		Ex. Given two pieces of data, place on a graph.
8.EE.6. Use similar triangles		Ex. Given a ratio of 3:1 indicating that each student needs three items,
to explain why the slope m		guide student in converting ratio to fraction form (2/1) and plot on a pre-
is the same between any		labeled graph.
two distinct points on a		
non-vertical line in the		Students will:
coordinate plane; derive		EE8.EE.5-6. Identify a specific data point when given the coordinates.
the equation y = mx for a		Ex. Read and plot coordinates on a map.
line through the origin and		Ex. Given three widespread data points and coordinates, identify named
the equation $y = mx + b$ for		point.
a line intercepting the vertical axis at b.		Ex. Given a standard multiplication chart, find the product of two numbers using coordinate skills.
		Ex. Indicate with coordinates what data points mean or the data revealed
		by the specify point.
		Students will:
		EE8.EE.5-6. Place or locate data on a simple two-category graph.
		Ex. Use distance landmark to tell if something is close or far away.
		Ex. Finds objects after movement (searches a small area comprehensively).
		Ex. Locate objects on a map (with or without coordinates).
Analyze and solve linear		Students will:

AK Grade-Level Clusters	AK-DLM Essential Elements	Instructional Examples

AK Grade-Level Clusters	AK-DLM Essential Elements	Instructional Examples

AK Grade-Level Clusters	AK-DLM Essential Elements	Instructional Examples



Eighth Grade Mathematics Standards: Functions

AK Grade-Level Clusters	AK-DLM Essential Elements	Instructional Examples
Define, evaluate, and compare functions.	EE8.F.1-3. Given a function table containing at least 2 complete ordered pairs,	Students will: EE8.F.1-3. Given a function table, identify the rule and express the rule for the missing variable (e.g., n times 2).
8.F.1. Understand that a function is a rule that	identify a missing number that completes another	Ex. Given a function table, identify the rule to find the missing number.
assigns to each input exactly one output. The graph of a function is the	ordered pair (limited to linear functions).	1 2 3 4 n 2 4 6 8 X
set of ordered pairs consisting of an input and the corresponding		Ex. Given a function table, identify the rule to find the missing number.
output. 19		1 2 3 4 n 5 10 15 20 X
8.F.2. Compare properties of two functions each represented in a different		Students will: EE8.F.1-3. Given a function table, identify the missing number. Ex.
way (algebraically, graphically, numerically in tables, or by verbal		1 2 3 4 2 4 X 8
descriptions). For example, given a linear function represented by a table of values and a linear function represented by an algebraic expression, determine which function has the greater rate of		Students will: EE8.F.1-3. Identify the relationship between two numbers. Ex. Given choices, tell the relationship between two numbers (e.g., How much more is five than three? Five is two more than three). Ex. Identify the relationship between two given numbers (e.g., If you double four, you have eight). Students will:
change.		EE8.F.1-3. Given a sequence, match the element of a sequence.

¹⁹ Function notation is not required in Grade 8.

AK Grade-Level Clusters	AK-DLM Essential Elements	Instructional Examples
8.F.3. Interpret the		Ex. Given the sequence 1, 2, 1, 2 and a 1, match to number 1.
equation $y = mx + b$ as		Ex. Given a sequence of triangle, circle, triangle, circle and a circle, match
defining a linear function,		the circle.
whose graph is a straight		
line; give examples of		
functions that are not		
linear. For example, the		
function $A = s^2$ giving the		
area of a square as a		
function of its side length is		
not linear because its		
graph contains the points		
(1,1), (2,4) and (3,9), which		
are not on a straight line.		
Use functions to model	EE8.F.4. Determine the	Students will:
relationships between	values or rule of a function	EE8.F.4. Given the input values and a rule, complete the output.
quantities.	using a graph or a table.	Ex. Complete the table by adding three to each input value.
8.F.4. Construct a function		x y
to model a linear		1
guantities Determine the		2
quantities. Determine the rate of change and initial		3
value of the function from		4
a description of a		
relationship or from two (x,		Students will:
y) values, including reading		EE8.F.4. Determine the values or rule of a function using a graph or a
these from a table or from		table.
a graph. Interpret the rate		Ex. Given a table, determine rule applied.
of change and initial value		
of a linear function in		x y
terms of the situation it		1 1+ = 4
models, and in terms of its		

AK Grade-Level Clusters	AK-DLM Essential Elements	Instructional Examples
graph or a table of values.		2 2+ _ = 5
		3 3+_= 6
		Ex. Given a table, determine increase or decrease.
		х у
		1 4
		2 5
		3 6
		Students will:
		EE8.F.4. Navigate, read, use, or apply a graph or table.
		Ex. Given a set of coordinates, locate on a graph. Ex. Given a location, identify coordinates.
		Ex. Using a basic map of town, identify two streets over.
		Students will:
		EE8.F.4. Identify the different parts of a graph or a table.
		Ex. Recognize more or less.
		Ex. Recognize a graph.
		Ex. Recognize a table. Ex. Identify rows/columns.
8.F.5. Describe	EE8.F.5. Describe how a	Students will:
qualitatively the functional	graph represents a	EE8.F.5. Describe how a graph represents a relationship between two
relationship between two	relationship between two	quantities and use the graph to answer questions using that relationship.
quantities by analyzing a graph (e.g., where the function is increasing or	quantities.	Ex. Given a chart showing the numbers of each colored disk in a bag, show how the graph relates color to number (e.g., point to the axis that tells you the number and to the axis that tells you the color and point to the bar

AK Grade-Level Clusters	AK-DLM Essential Elements	Instructional Examples
decreasing, linear or nonlinear). Sketch a graph that exhibits the qualitative features of a function that has been described verbally.		that shows the color with the highest number). Ex. Given a line graph showing days of consecutive snowfall and inches of accumulated snow, show how the graph relates number of days to amount of accumulated snow (e.g., say the name of the axis that shows inches of snow and the axis that show consecutive days of snowfall and then tell which point on the graph shows the most snow and most consecutive days of snowfall). Students will: EE8.F.5. Describe how a graph represents a relationship between two quantities. Ex. Given a chart showing the numbers of each colored disk in a bag, show how the graph relates color to number (e.g., point to the axis that tells you the number and to the axis that tells you the color). Ex. Given a line graph showing days of consecutive snowfall and inches of accumulated snow, show how the graph relates number of days to amount of accumulated snow (e.g., say the name of the axis that shows inches of snow and the axis that shows consecutive days of snowfall). Students will: EE8.F.5. Answer questions about data from a graph. Ex. Given a chart of colors in an M&M bag, answer a question about the information on the graph (e.g., Which is the most common color?). Ex. Given a bar graph representing numbers of colored disks found in a
		bag, answer a question about the information (e.g., A bag of colored discs contains 15 red, 12 blue, eight green, and five yellow. Which bar shows how many red discs are in the bag?). Ex. Given a picture graph showing a five-day forecast showing snow showers for all days, identify which point shows how much snow is expected to fall on the fifth day. Students will:
		EE8.F.5. Place data in a graph.

AK Grade-Level Clusters	Common Core Essential Elements	Range of Complexity Examples
		Ex. Place stickers of the same type (e.g., color, animal) on the same bar in a graph? Ex. Group data into categories and place on a graph (e.g., types of music, types of food).



Eighth Grade Mathematics Standards: Geometry

AK Grade-Level Clusters	AK-DLM Essential Elements	Instructional Examples
Understand congruence	EE8.G.1. Recognize	Students will:
and similarity using	translators, rotations, and	EE8.G.1-3. N/A
physical models,	reflections of shapes.	
transparencies, or		Students will:
geometry software.	EE.8.G.2. Identify shapes that are congruent.	EE8.G.1-3. Identify similarity and congruence (same) in objects and shapes containing angles without translations.
8.G.1. Verify		Ex. Match an angle in one shape with the same angle in another shape
experimentally the		with manipulatives or pictures.
properties of rotations,		Ex. Given different size shapes, find the two shapes that are similar and tell
reflections, and		why.
translations:		Ex. Given a picture of a shape, match that picture to the congruent object
a. Lines are taken to lines,		on the table.
and line segments to		Ex. Using a picture of a door at a 45- or 90-degree angle adjust the
line segments of the		classroom door to the same angle.
same length.		
b. Angles are taken to		Students will:
angles of the same		EE8.G.1-3. Match similar shapes.
measure.		Ex. Match a square to a square.
c. Parallel lines are taken		Ex. Match a large square with a large square.
to parallel lines.		Ex. Given shapes, find the two shapes that are similar and tell why.
8.G.2. Understand that a		Students will:
two-dimensional figure is		EE8.G.1-3. Match shapes using a three-dimensional object.
congruent to another if the		Ex. Overlay the outline of a shape with a three-dimensional object using
second can be obtained		angles in the outline as guides (e.g., building with blocks).
from the first by a		Ex. Tell, which socks match in color, shape, and size.
sequence of rotations,		Ex. If a sock is upside down and another sock is right side up, can you make
reflections, and		them match?
translations; given two		
congruent figures, describe		
a sequence that exhibits		
the congruence between		

AK Grade-Level Clusters	AK-DLM Essential Elements	Instructional Examples
them.		
8.G.4. Understand that a two-dimensional figure is similar to another if the second can be obtained from the first by a sequence of rotations, reflections, translations, and dilations; given two similar two-dimensional figures, describe a sequence that exhibits the similarity between them.	EE8.G.4. Identify similar shapes with and without rotation.	Students will: EE8.G.4. Determine if geometric shapes are similar with rotations or reflections. Ex. Sort shapes into groups of similar shapes with rotation and similar shapes with reflections. Ex. Matches combinations of similar shapes to each other (e.g., match similar shapes with rotations to each other and match similar shapes with reflections to each other). Students will: EE8.G.4. Identify similar shapes with and without rotation. Ex. Given a shape find its similar rotation. Ex. Compare shapes in the environment to find a similar shape that is rotated.
		Ex. When given a group of triangles, select two that are similar when one is rotated. Ex. Select the shape that is not similar from a group of three shapes. Students will: EE8.G.4. Identify similar geometric shapes. Ex. Sort regular polygons into groups of similar shapes. Ex. When given a shape, select a similar shape. Ex. Match the shape of one small square to the shape of a large square. Students will: EE8.G.4. Recognize geometric shapes. Ex. Same thing comparer – compare to shapes to see if they are the same.

AK Grade-Level Clusters	AK-DLM Essential Elements	Instructional Examples
		Ex. Select the named shape. Ex. When shown a shape, name the shape. Ex. Point to a triangle when shown a circle and a triangle. Ex. Trace around a geometric shape.
arguments to establish facts about the angle sum and exterior angle of triangles, about the angles	angle to a right angle, and describe the angle as greater than, less than, or congruent to a right angle.	Students will: EE8.G.5. Compare measures of angles formed by intersecting lines. Ex. Given intersecting lines, identify linear pair angles. Ex. Given a pair of parallel lines intersected by a third line, identify angles that are the same measure. Students will: EE8.G.5. Compare measures of angles to a right angle (greater than, less than, or equal to). Ex. Locate an angle with a measure greater than the measure of a right angle. Ex. Use a right-angle tool (square corner - corner of a note card), to find right angles. Students will: EE8.G.5. Recognize a right angle. Ex. Identify a right angle in the school environment. Ex. Which of these is a right angle? Ex. Teacher creates on a geoboard. Is this a right angle? Students will: EE8.G.5. Recognize an angle. Ex. Find angles in given shapes. Ex. Find a corner in the classroom (e.g., corner of the room or a table).

AK Grade-Level Clusters	AK-DLM Essential Elements	Instructional Example
		Students will: EE8.G.9. Apply knowledge of volume. Ex. Use simple units to fill a container with accurate counting. Ex. Uses cubes to fill a small container and estimate the number of cubes it took by mathematical reasoning (addition or multiplication of row/column). Ex. Select appropriate tool to fill a pitcher (e.g., tsp., cup, bucket). Ex. Select appropriate tool to measure flour for a cake – cup or bucket. Ex. Convert – how many cups in a pint?
Solve real-world and mathematical problems involving volume of cylinders, cones, and spheres. 8.G.9. Know the formulas for the volumes of cones, cylinders, and spheres and use them to solve real-world and mathematical problems.	common measures (cups, pints, quarts, gallons, etc.).	Students will: EE8.G.9. Identify volume of common measures (cups, pints, gallons, etc.). Ex. Tell which holds more when using cubes to fill two boxes (e.g., count the cubes that fit in one box as compared to another). Ex. Identify which is a cup when given a cup, teaspoon, and a gallon container. Ex. Show which is a gallon when given a teaspoon, ball, and a gallon

AK Grade-Level Clusters	AK-DLM Essential Elements	Instructional Examples
		container.
		Ex. Given a gallon, tell if it will take longer to fill the gallon with cups or
		with pints?
		Students will:
		EE8.G.9. Identify which is more or less?
		Ex. Compares two containers using a third for transitive reasoning – pours
		one container into two others to see which holds more because one may
		overflow and one may not become full.
		Ex. Which container has more marbles in it?
		Ex. Which container has less marbles in it?
		Students will:
		EE8.G.9. Experience volume.
		Ex. Compare two containers – which holds more?
		Ex. Point to the empty cup.
		Ex. Point to the full container.

Eighth Grade Mathematics Standards: Statistics and Probability

AK Grade-Level Clusters	AK-DLM Essential Elements	Instructional Examples

AK Grade-Level Clusters	AK-DLM Essential Elements	Instructional Examples
8.SP.4. Understand that patterns of association can also be seen in bivariate categorical data by displaying frequencies and relative frequencies in a two-way table. Construct and interpret a two-way table summarizing data on two categorical variables collected from the same subjects. Use relative frequencies calculated for rows or columns to describe possible association between the two variables. For example, collect data from students in your class on whether or not they have a curfew on school nights and whether or not they have assigned chores at home. Is there	EE8.SP.4. Construct a graph or table from given categorical data and compare data categorized in the graph or table.	Students will: EE8.SP.4. Conduct an experiment, collect data, and construct a graph or table. Ex. Conduct an experiment to find if plants grow faster in the sun or in the shade. Graph plant height over time and make a conclusion. Ex. Ask 10 people how many hours of TV they watch a day. Put the findings into a table. Students will: EE8.SP.4. Construct a graph or table from given categorical data and compare data categorized in the graph or table. Ex. Given data about boys' and girls' favorite games, create a bar graph and compare the preferences of boys and girls. Ex. Given two graphs (hours of TV watched by boys and hours of TV watched by girls), answer questions to compare the habits of each. Students will: EE8.SP.4. Collect and organize data. Ex. Organize objects into groups (teddy bears, balls, crayons). Ex. Examine a basic bus route schedule in table form and highlight which buses run at 5:00 p.m. Ex. Given five students, organize them shortest to tallest.

AK Grade-Level Clusters	AK-DLM Essential Elements	Instructional Examples
evidence that those who have a curfew also tend to have chores?		Students will: EE8.SP.4. Organize data into groups. Ex. Survey five people and ask if they like hamburgers or pizza better. Keep track of the findings. Ex. Organize disks by color and count how many of each. Which is most and which is least? Ex. Organize clothing by type (e.g., shirt, pants, socks) and count how many of each. Which is most and which is least?

